

## **Dottorato in Metodi Matematici e Statistici per le Scienze Economiche e Sociali**

**Probability Theory:** definitions and concepts; conditional probability and independence; Bayes theorem; calculus of probabilities.

**Random variables:** definitions; expectations; mean and variance; *moments and moment generating functions\**; common families of distributions; *exponential families\**; *location and scale families\**.

**Multiple random variables:** joint, marginal and conditional distributions; independence; covariance and correlation; *most common families of multiple random variables\**.

**Some properties of probability distributions:** joint distribution of two random variables; Student's  $t$  and Fisher's  $F$  distribution; linear transformations of random variables; *most common inequalities and identities\**.

**Convergence concepts:** *laws of large numbers\**, *central limit theorems\**, *different types of convergence\**.

**Properties of random samples:** basic concepts of random samples; *different approaches to statistical inference\**; statistics based random samples; sampling from the normal and Bernoulli distribution; *principles of data reduction\**: *sufficiency*, *likelihood and invariance principles*.

**Point and interval estimation:** methods of finding estimators; methods of evaluating estimators; confidence intervals; confidence interval for: the mean of a normal and of a Bernoulli population, the difference of the means of two normal or Bernoulli populations, the variance of a normal population; confidence intervals for large samples.

**Hypothesis testing:** methods of finding tests; methods of evaluating tests; testing hypothesis for: the mean and of a normal and a Bernoulli population, the difference of the means of two normal or Bernoulli populations, the variance of a normal population; *large samples tests\**; *robustness of tests\**; *elements of nonparametric tests\**.

**Linear regression model:** simple linear regression model: interpretation of the model; point and interval estimation of the parameters; testing hypothesis on the

parameters; *multiple regression model*\*: *point and interval estimation of the parameters; testing hypothesis on the parameters.*

**References:**

Casella G. Berger R.L. (2002). *Statistical Inference*. Seconda Edizione. Wadsworth & Brooks Cole. Cap 1-9, Sec. 10.1, 11.2, 12.1.